

Green & Ampt equation

The penetration depth of the infiltrating wetting front is Z at any moment in time t . If we assume that the wetting front is a sharp Dirac delta-function, Darcy's law can be stated as follows:

$$q = \frac{dl}{dt} = -K_s * \left[\frac{h_f - (h_s + Z)}{Z} \right]$$

where K_s is the hydraulic conductivity and $I(t)$ is the cumulative infiltration at time t that is equal to $Z * (\theta_s - \theta_0)$ (conservation of mass).

Using the above relation for $I(t)$ to eliminate Z and performing the integration yields,

$$I = K_s * t * (h_f - h_s) * (\theta_s - \theta_0) * \log_e \left(1 - \frac{I}{(h_f - h_s) * (\theta_s - \theta_0)} \right)$$

with $I(t)$ infiltration amount in [cm], K_s hydr. conductivity in [cm/h], h_f wetting front pressure head (negative) in [cm], h_s water pressure at surface (ponding) in cm, θ_s moisture content at saturation, θ_0 antecedent moisture.

In order to solve this implicit equation, we need to bring $I(t)$ to one side of the equation:

$$\frac{1}{K_s} * \left[I - (h_f - h_s) * (\theta_s - \theta_0) * \log_e \left(1 - \frac{I}{(h_f - h_s) * (\theta_s - \theta_0)} \right) \right] = t$$

We can then insert I can calculate t - we calculate the time that corresponds to a given infiltration amount. An R-code to calculate infiltration amounts with Green & Ampt looks like this:

[|Green-Ampt.R](#)

```
I      <- seq(0,100,by=1.0)
t0     <- 0.05
ts     <- 0.25
hs     <- 0.0 # cm
hf     <- -12.0 # cm
Ks     <- 8.0 # cm/hour
t      <- 1/Ks*((I-(hf-hs)*(ts-t0))*log(1-(I/((hf-hs)*(ts-t0))))
# hours
plot(t,I,xlim=c(0,6),ylim=c(0,25),xlab="t [hour]", ylab="I in
[cm]")
```

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Last update: **2024/04/10 10:02**

